

$\Lambda^* = h/D(m\epsilon^*)^{\frac{1}{2}}$  which de Boer<sup>11,12</sup> showed occurs in the general expression for the reduced equation of state in quantum statistics. Eqn. (2) then becomes

$$\Delta p^* = T^* \left[ v^{*-1} + \frac{3}{2} \frac{d \log y^*}{d v^*} \right] [9.0710 y^{*\frac{1}{2}} T^{*\frac{1}{2}} v^{*\frac{1}{2}} \Lambda^{*-1} - 1]^{-1}, \quad (3)$$

where  $y^*$  is a function of  $v^*$ , the relationship between them being

$$(1 + 12y^* + 25.2y^{*2} + 12y^{*3} + y^{*4})(1 + y^*)^{-1}(1 - y^*)^{-6} - 2v^{*2} = 0. \quad (4)$$

Thus, in conformity with the general considerations of de Boer<sup>11,12</sup> our reduced quantal equation of state is of the type

$$p^* = f(T^*, v^*, \Lambda^*),$$

where  $f$  is a universal function.

For the general plot of  $p^*$  against  $v^*$  in fig. 4, we have selected the reduced temperature  $T^* = 2.14$  corresponding to our experimental temperature  $T = 78.9^\circ \text{K}$ .

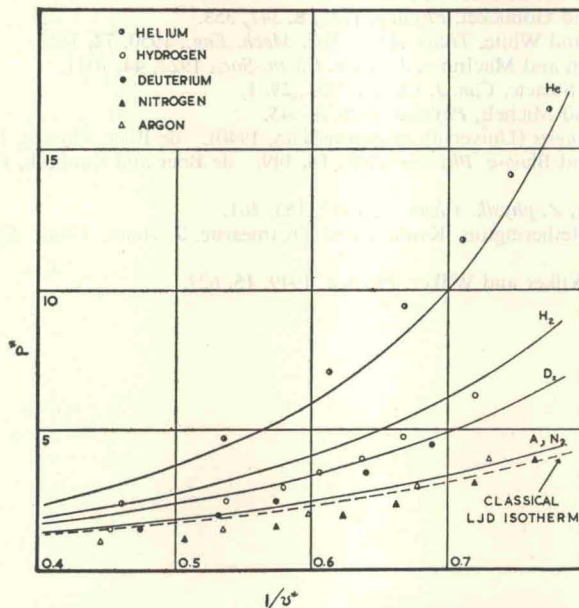


FIG. 4.—Reduced isotherms for  $T^* = 2.14$ . The full curves are the quantal isotherms.

TABLE 3.—MOLECULAR CONSTANTS

	$\epsilon^*/k$ ( $^\circ\text{K}$ )	$D$ ( $\text{cm} \times 10^{-8}$ )	$\Lambda^*$
He	10.2	2.56	2.64
H <sub>2</sub>	37.0	2.92	1.73
D <sub>2</sub>	37.0	2.92	1.22
N <sub>2</sub>	96.6	3.72	0.225
A	120.3	3.41	0.187

for H<sub>2</sub> and D<sub>2</sub>. The intermolecular force parameters and the values of  $\Lambda^*$  have been taken from the tables of de Boer.<sup>11,12</sup> They are listed in table 3. The experimental data for He, N<sub>2</sub> and A were given by short extrapolations on the temperature scale from the measurements of Buchmann<sup>13</sup> on He; Bartlett, Hetherington, Kvalnes and Tremearne<sup>14</sup> on N<sub>2</sub>; Michels, Wijker and Wijker<sup>15</sup> on A.

Fig. 4 shows that the isotherm given by the classical theory is a fairly good representation of the behaviour of the heavy gases  $N_2$  and A, and that the predicted differences between the quantal isotherms are in good agreement with the experimental differences between the light gases.

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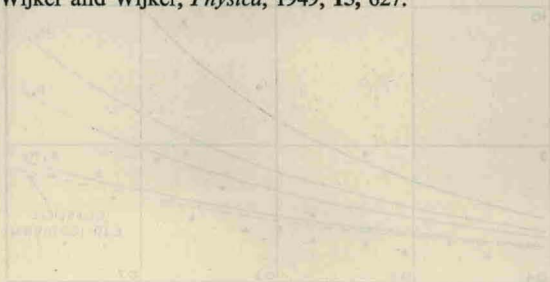


Fig. 4.—Reduced isotherms for  $V/V_0 = 200$ . The full curves are the classical isotherms.

TABLE 5. MOLECULAR WEIGHTS

Gas	Molecular Weight	Gas	Molecular Weight
A	130.1	H <sub>2</sub>	2.02
N <sub>2</sub>	28.0	D <sub>2</sub>	4.04
H <sub>2</sub>	2.02	H <sub>2</sub>	2.02
D <sub>2</sub>	4.04	H <sub>2</sub>	2.02
H <sub>2</sub>	2.02	H <sub>2</sub>	2.02
H <sub>2</sub>	2.02	H <sub>2</sub>	2.02

for H<sub>2</sub> and D<sub>2</sub>. The intermolecular force parameters and the values of  $\mu$  have been taken from the tables of de Boer<sup>11</sup>. They are listed in table 5. The experimental data for H<sub>2</sub> and A were given by their contributors on the basis of the measurements of the isotherms on the isothermometer of Hetherington, Kvalnes and Treamearne<sup>14</sup> and Wijker and Wijker<sup>15</sup>.